

# Ferroelectric Homogenized Energy Polarization Model

[http://www.leapcad.com/Ferroelectrics/Polarization\\_Homogenized\\_Energy.mcd](http://www.leapcad.com/Ferroelectrics/Polarization_Homogenized_Energy.mcd)

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Polarization\_Model\_DemoMC



### Model Type, Assumptions, and Data:

Discretized Macroscopic Model with 4-point Gauss-Legendre Quadrature Rule  
Lognormal/Normal Density(2), No Thermal Relaxation(0)

dat := READPRN("http://www.leapcad.com/Ferroelectrics/params\_pzt\_log\_demo.dat")

$$C := \text{dat}_2 \quad E_{c\_bar} := \text{dat}_3 \quad c := \text{dat}_4 \quad c_1 := \sqrt{C} \quad b_2 := \text{dat}_5 \quad E_{c\_int} := E_{c\_bar} \cdot 200^c \quad E_{i\_int} := \sqrt{b_2 \cdot 7}$$

$$C = 1.417 \times 10^{-12} \quad E_{c\_bar} = 7.581 \times 10^5 \quad c = 0.239 \quad c_1 = 1.191 \times 10^{-6} \quad b_2 = 2.985 \times 10^{10}$$

$$E_{c\_int} = 2.696 \times 10^6 \quad E_{i\_int} = 4.571 \times 10^5 \quad \mu := 10^{-6} \quad \epsilon_0 := 8.854 \cdot 10^{-12} \cdot \frac{\text{r}}{\text{m}} \quad M := 10^6$$

### Model Solution Results Output to "PolarOutput File"

PFile := READPRN("http://www.leapcad.com/Ferroelectrics/PolarOutput2.txt")

E := submatrix(PFile, 1, 1461, 1, 1) · 10<sup>-6</sup>

P := submatrix(PFile, 1462, 2922, 1, 1) · 100

#### Coercive and Interactive Fields: Ec and Ei

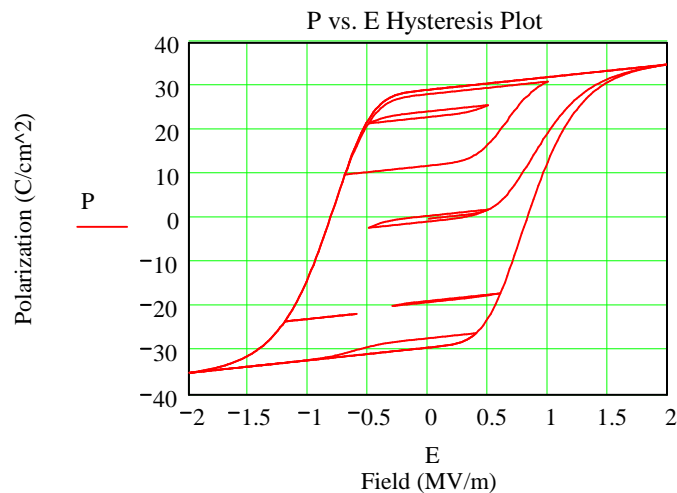
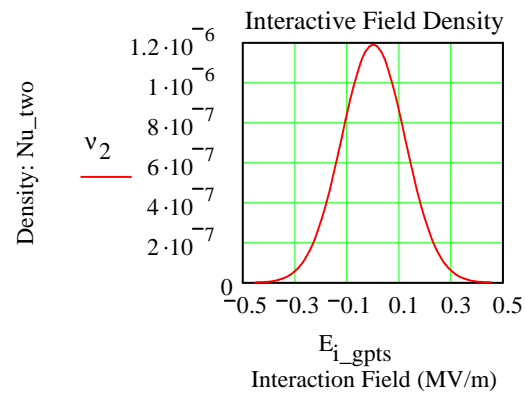
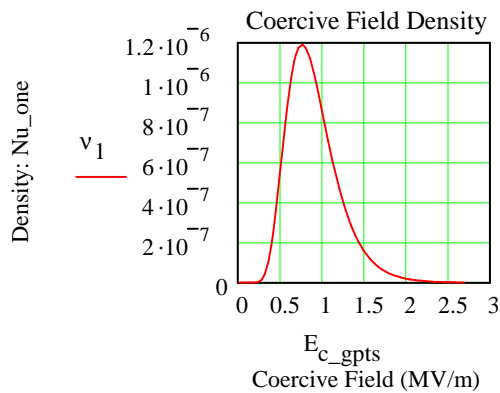
E<sub>c\_gpts</sub> := submatrix(PFile, 2923, 3002, 1, 1) · 10<sup>-6</sup>

#### Density Calculations: v1 and v2

v<sub>1</sub> := submatrix(PFile, 3003, 3082, 1, 1)

E<sub>i\_gpts</sub> := submatrix(PFile, 3164, 3243, 1, 1) · 10<sup>-6</sup>

v<sub>2</sub> := submatrix(PFile, 3084, 3163, 1, 1)



R := rows(E)    n := 1..R - 2    u := 1031..931

$$k_n := \frac{1}{\epsilon_0} \cdot \left( \frac{P_{n+1} - P_n}{E_{n+1} - E_n} \right) \cdot \frac{\mu \cdot \text{coul}}{\text{cm}^2} \cdot \frac{\text{m}}{\text{M} \cdot \text{V}} \quad \kappa_u := k_u$$

